

Systems of Equations - Substitution

SEQ

Substituting an expression from one equation for a variable in another equation

Steps:

- 1) Solve one of the equations for one of its variables (when possible choose a variable with a coefficient of one or negative one)
- 2) Substitute the expression from step one into the other equation and solve for the other variable
- 3) Substitute the value from step two into an original equation and solve.
- 4) Check your answer (x,y) in BOTH original equations

Example:

$$\begin{cases} 8x + 2y = 19 \\ x = 3 \end{cases}$$

plug the value for x from one equation into the other equation & solve for y

$$\begin{aligned} 8(3) + 2y &= 19 \\ 24 + 2y &= 19 \\ -24 &\quad -24 \\ 2y &= -5 \\ y &= -2.5 \end{aligned}$$

x=3, y=-2.5 Solution: (3, -2.5)

Example:

$$\begin{cases} 15x - 5y = 30 \\ y = 2x + 3 \end{cases}$$

$$15x - 5(2x + 3) = 30$$

$$15x - 10x - 15 = 30$$

$$y = 2x + 3$$

$$y = 2(9) + 3$$

$$y = 18 + 3$$

$$y = 21$$

$$5x - 15 = 30$$

$$+ 15 \quad + 15$$

$$5x = 45$$

$$x = 9$$

$$(9, 21)$$

Ex:

$$\begin{cases} 2x - y = 23 \\ x - 9 = -1 \end{cases}$$

$$x = 8$$

$(8, -7)$

$$2(8) - y = 23$$

$$16 - y = 23$$

$$-y = 7$$

$$y = -7$$