

## Geometric Sequences

EXP

Geometric Sequence: the ratio of any term to the previous term is constant (multiplied by same number each term)

(Exponential Growth or Decay)

common ratio: the constant ratio ( $r$ )

$n$ th term of a geometric sequence:  $a_n = a_1 r^{n-1}$

$$a_n = a_1 \cdot r^{n-1}$$

EX: 128, 64, 32, 16, 8..... find the 7th term

$$r = \frac{1}{2} \quad a_1 = 128$$

$$a_7 = 128 \cdot \left(\frac{1}{2}\right)^6$$

$$a_7 = 128 \left(\frac{1}{64}\right) = 2$$

to find  $r$ :  $\frac{a_2 \text{ (2nd term)}}{a_1 \text{ (1st term)}}$

## Recursive Rules

recursive rule - gives the beginning term(s) of a sequence

recursive equation - tells how  $a_n$  relates to the previous terms

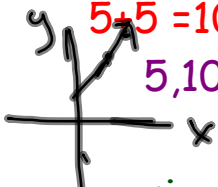
recursive equation for arithmetic sequences:  $a_n = a_{n-1} + d$    
 EX:  $a_1 = 5, a_n = a_{n-1} + 5$ , give the first six terms of the sequence

→ linear

$n^{\text{th}}$  term = sum of previous term + common difference

$$5+5=10, 10+5=15, 15+5=20, 20+5=25, 25+5=30$$

5, 10, 15, 20, 25, 30



→ exponential

$n^{\text{th}}$  term = product of previous term & common ratio

recursive equation for geometric sequences:  $a_n = r \cdot a_{n-1}$    
 EX:  $a_1 = 1, a_n = 2 \cdot a_{n-1}$ , give the first six terms of the sequence

$$2 \cdot 1 = 2, 2 \cdot 2 = 4, 2 \cdot 4 = 8, 2 \cdot 8 = 16, 2 \cdot 16 = 32$$

1, 2, 4, 8, 16, 32

